

11 Vectors and the Geometric of Space

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Outline of Chapter 11

- 1 Three-Dimensional Coordinates Systems
- 2 Vectors and Vector Algebra
- 3 The Dot Product
- 4 The Cross Product
- 5 Describing Lines and Planes

11.1 Three-Dimensional Coordinates Systems

- The coordinates in a three dimensional system are of the form (x,y,z) , called the ordered triple.
- A point P is located at $(x,y,z) \Rightarrow P(x,y,z)$.
- The Cartesian product $\mathbb{R}^3 = \mathbb{R} \times \mathbb{R} \times \mathbb{R} = \{(x,y,z) | x,y,z \in \mathbb{R}\}$

Example1

Describe the region of \mathbb{R}^3 represented by the equation or inequality.

1. $z = 1$
2. $x^2 + y^2 + z^2 \leq 4$

- The Distance between $P_1(x_1, y_1, z_1)$ and $P_2(x_2, y_2, z_2)$ is

$$|\overline{P_1P_2}| = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2 + (z_1 - z_2)^2}.$$

Example2

Find the distance between $P_1(1,2,3)$ and $P_2(-3,-1,0)$.

- The Standard Equation for a Sphere with Radius r and Center (x_0, y_0, z_0) is

$$(x - x_0)^2 + (y - y_0)^2 + (z - z_0)^2 = r^2$$

Example3

Find the center and radius of the sphere.

1. $x^2 + y^2 + z^2 + 4x - 6z + 3 = 0$

2. $2x^2 + 2y^2 + 2z^2 = -8x + 24y + 2$